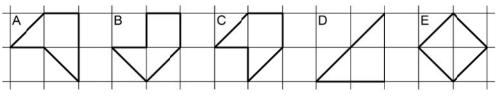
## Mathematics Kangaroo 2012 Group Junior (Grades 9./10.) Austria - 15.3.2012



## - 3 Point Questions -

**1.** Which of the shapes to the right has the largest area?



- (A) A
- (B) B
- (C) C
- (D) D
- (E) All shapes have the same area.

**2.** 11.111-1.1111=

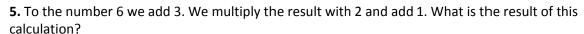
- (A) 9.0009
- (B) 9.0909
- (C) 9.9999
- (D) 9.999
- (E) 10

**3.** A wristwatch was laid on a table in such a way that the minute hand pointed northeast. How many minutes must pass before the minute hand is pointing northwest for the first time?

- (A) 45
- (B) 40
- (C)30
- (D) 20
- (E) 15

**4**. M and N are the midpoints of the equal sides of an isosceles triangle. How big is the area of the quadrilateral (marked ?)?

- (A) 3
- (B) 4
- (C) 5
- (D) 6
- (E) 7



- (A) 27
- (B) 7
- (C) 18
- (D) 20
- (E) 19

**6.** A cuboid is formed from 3 pieces (see picture). Each piece is made from 4 cubes of the same colour. What shape does the white piece have?

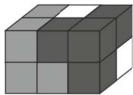












7. The digit sum of a seven digit number is 6. What is the product of the digits?

- (A) 0
- (B)6
- (C) 7
- (D)  $1\times2\times3\times4\times5\times6\times7$
- (E) 5

**8.** ABC is a right-angled triangle with shorter sides 6cm and 8cm. K, L, M are the midpoints of the sides of triangle ABC. What is the perimeter of triangle KLM?



(A) 10 cm

- (B) 12 cm
- (C) 15 cm
- (D) 20 cm
- (E) 24 cm

**9.** The quadrilateral ABCD with side length 4cm has the same area as triangle ECD. What is the perpendicular distance from point E to the line g?



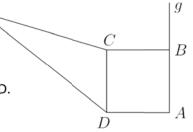
- (B)  $(4 + 2\sqrt{3})$  cm
- (C) 12 cm

(D)  $10 \times \sqrt{2}$  cm

(E) It depends on the position of E.

**10.** Alice and Bob send each other secret messages. To put their messages into code they use the following system: First each letter is given a number in order: A = 1, B = 2, C = 3, ... Z = 26. Then the letter number is doubled and 9 is added. Bob received a message which began 19 - 37 - 48 - 19 - ... Which of the following messages had Alice sent to Bob?

- (A) ENDE...
- (B) ENTE...
- (C) ERNA...
- (D) ERDE...
- (E) Alice has made a mistake



## - 4 Point Questions -

11. In four of the following calculations you can swap the number 8 with another positive number without changing the answer to the sum. For which calculation does it not work?

(A) 
$$(8+8-8) \div 8$$

(B) 
$$8 + (8 \div 8) - 8$$

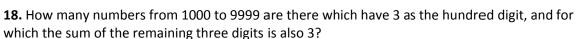
(C) 
$$8 \div (8 + 8 + 8)$$

(D) 
$$8 - (8 \div 8) + 8$$

(E) 
$$8 \times (8 \div 8) \div 8$$

- 12. When Adam stands on a table and Mike on the floor, Adam is 80cm taller than Mike. When Mike stands on the table and Adam on the floor, Mike is one metre taller than Adam. How high is the table?
- (A) 20 cm
- (B) 80 cm
- (C) 90cm
- (D) 100 cm
- (E) 120 cm
- 13. When the numbers 144 and 220 are divided by the same positive whole number x, both have remainder 11. Find x.
- (A) 7
- (B) 11
- (C) 15
- (D) 19
- (E) 38
- 14. Tom and Mary play a game with a coin. When the coin shows heads, Mary wins and Tom must give her two sweets. When the coin shows tails Tom wins and Mary must give him three sweets. After 30 throws of the coin they each have the same number of sweets as they had at the start of the game. How often has Tom won?
- (A) 6
- (B) 12
- (C) 18
- (D) 24
- (E) 30
- 15. One of the two sides of a rectangle has length 6cm. In the rectangle circles are drawn next to each other in such a way that their centres form an equilateral triangle. What is the shortest distance between the two grey circles (in cm)?
- (A) 1
- (B)  $\sqrt{2}$
- (C)  $2\sqrt{3} 2$  (D)  $\frac{\pi}{2}$

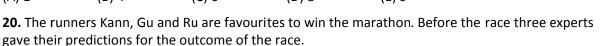
- 16. On each of the four walls in Billy's room hangs a correctly working clock, but each one runs either behind or ahead of the correct time. The first clock is incorrect by 2 minutes, the second by 3 minutes, the third by 4 minutes and the fourth by 5 minutes. Billy wants to know what time it is and sees the following times; 6 minutes to 3, 3 minutes to three, 2 minutes past three and 3 minutes past 3. What is the actual time?
- (A) 3:00
- (B) 2:57
- (C) 2:58
- (D) 2:59
- (E) 3:01
- 17. The diagram shows a right-angled triangle with side lengths 5, 12 and 13, What is the length of the radius of the inscribed semi-circle?
- (A) 7/3
- (B) 10/3
- (C) 12/3
- (D) 13/3
- (E) 17/3



- (A) 2
- (B) 3
- (C) 4
- (D) 5
- (E) 6
- 19. A number from 1 to 9 is to written into each of the 12 fields of the table so that the sum of each column is the same. Also the sum of each row must be the same. A few numbers have already been written in. Which number should be written in the grey square?



- (B) 4
- (C) 6
- (D) 8
- (E)9



- Expert 1: "Either Kann or Gu will win."
- Expert 2: "If Gu is second Ru will win."
- Expert 3: "If Gu is third Kan will not win."
- Expert 4: "Either Gu or Ru will come second."

After the race all four predictions were proven correct. In which order, did the three runners finish the race?

- (A) Kan, Gu, Ru
- (B) Kan, Ru, Gu
- C) Ru, Gu, Kan
- (D) Gu, Ru, Kan
- (E) Gu, Kan, Ru



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## - 5 Point Ouestions -

(A) 16

(B) 8

3 I offit Questions									
<b>21.</b> Two sides of a quadrilateral have lengths 1 and 4. On quadrilateral into two isosceles triangles. What is the property (A) 8 (B) 9 (C) 10 (D) 11			the qu		_		d split	s the	
22. A goldsmith has 12 double-links of chain. Out of these he wants to make a single closed chain with 24 links. What is the minimum number of links that he must open (and close again)?  (A) 8 (B) 9 (C) 10 (D) 11	988				න න	E.	<u> </u>	D. DO	000 000
<b>23.</b> Peter wrote the number 2012 in the form 2012 = m. Find the value of k.  (A) 2 (B) 3 (C) 4 (D) 9	n <sup>m</sup> (m <sup>k</sup> ·	– k) w (E)		n and l	k are r	natura	l num	bers.	
<b>24.</b> What is the last non zero digit of K = $2^{59} \times 3^4 \times 5^{53}$ ? (A) 1 (B) 2 (C) 4 (D) 6	?	(E)					M		
25. A rectangle ABCD with dimensions 16cm by 4cm we the line MN so that corner C meets corner A. What is to Pentagon ABNMD'?  (A) 17 cm <sup>2</sup> (B) 27 cm <sup>2</sup> (C) 37 cm <sup>2</sup> (D) 47 cm <sup>2</sup>	he are	a of th	ne	3		N			
<b>26.</b> It takes 8 seconds for train G to pass by a milestone takes 9 seconds for the trains to pass each other. Train milestone. What can be deduced about the length of the second secon	H the	n take						H. It	
(A) G is twice as long as H. (B) They are the san (D) H is twice as long as G. (E) Nothing can be on		-	(0	C) H is	50% l	onger	than (	G	
27. The shape pictured, is made out of two squares with 5cm respectively, a triangle with area 8 cm <sup>2</sup> and the grather area of the parallelogram?  (A) 15 cm <sup>2</sup> (B) 16 cm <sup>2</sup> (C) 18 cm <sup>2</sup> (D) 20 cm <sup>2</sup>	ey par	allelog		What i	is $\angle$	4	<u> </u>		>
<b>28.</b> Of 5 lamps each one can be set to "ON" or "OFF". E changed, not only does the status of that particular land chosen at random. If the same switch is changed sever changes. Initially all lamps are set to "OFF". Then 10 swone can say that	np cha al time	inge b es not	ut also alway	that o	of one	other other l	r lamp lamp		
<ul><li>(A) definitely not all lamps are switched to "OFF";</li><li>(B) definitely all lamps are switched to "ON";</li></ul>	1								
(C) definitely not all lamps are switched to "ON";	2	3							
<ul><li>(D) definitely all lamps are switched to "OFF";</li><li>(E) none of the statements in (A) to (D) are true.</li></ul>	$\frac{4}{7}$	5 8	6 9	10					
<b>29.</b> The natural numbers from 1 to 120 were written	11	12	13	14	15				
as shown into a table with 15 columns. In which	:	:	:	:	:	:	:	J	:
column (counting from left) is the sum of the numbers the largest?	106	107	108	109	110	111	112	]	120
(A) 1 (B) 5 (C) 7 (D) 10 (E) 13									
<b>30.</b> Positive numbers were written in a $3 \times 3$ grid in suc	ch a wa	ay tha	t the p	roduc	t of th	e num	nbers i	in	

each row and each column is exactly 1. The product of the four numbers in each  $2 \times 2$  grid that can

(D)  $\frac{1}{4}$ 

(E)  $\frac{1}{8}$ 

be found inside the  $3 \times 3$  grid is 2. Which number is written in the centre of the  $3 \times 3$  grid?

(C) 4